Non-mandatory problem 5

Deadline: November 19th

Prove that $r^4\dot{\theta}^2 + r^4\dot{\varphi}^2\sin^2\theta$ remains constant along any geodesic of the Schwarzschild metric.