

1) In class we made the `fermat_fact(n)` function returning a factor of n using Fermat factorization. Employ `fermat_fact(n)` and `is_prime(n)` to define the functions¹:

a) (80%) `fermat_factor_a(n)` printing a (non-necessarily ordered) list of the prime factors of n repeated according multiplicities. For instance, for $n=630$ it could give `2,3,7,3,5`.

b) (+20%) `fermat_factor_b(n)` printing the factorization of n in the usual (ordered) way as in the function `factor` in Sage. For instance, for $n=630$ it has to give `2 * 3^2 * 5 * 7`.

2) In a library the PIN is a string, say `pin`, of three characters encrypted in the magnetic stripe as a number given by the formula

$$\text{Mod}(256^2 \cdot \text{ord}(\text{pin}[0]) + 256 \cdot \text{ord}(\text{pin}[1]) + \text{ord}(\text{pin}[2]), 18121121)^{7919}$$

What is the PIN corresponding to 16479305?

¹Please send the answer to this challenge by email to `fernando.chamizo@uam.es` in a text file or in a Sage worksheet. The part b) requires some knowledge of Python. There is a Python cheat sheet in my web site.